

# 1 Characterising the in-out asymmetry in visual crowding

2 Ramakrishna Chakravarthi<sup>1</sup>, Jirko Rubruck<sup>1</sup>, Nikki Kipling<sup>2</sup> and Alasdair D F Clarke<sup>2</sup>

3 1. School of Psychology, University of Aberdeen, UK

4 2. Department of Psychology, University of Essex, UK

5 Abstract

6 An object's processing is impaired by the presence of nearby clutter. Several distinct  
7 mechanisms, such as masking and visual crowding, are thought to contribute to such flanker-  
8 induced interference. It is therefore important to determine which mechanism is operational in  
9 any given situation. Previous studies have proposed that the in-out asymmetry (IOA), where a  
10 peripheral flanker interferes with the target more than a foveal flanker, is diagnostic of  
11 crowding. However, several studies have documented inconsistencies in the occurrence of this  
12 asymmetry, particularly at locations beyond the horizontal meridian, casting doubt on its ability  
13 to delineate crowding. In this study, to determine if IOA is diagnostic of crowding, we  
14 extensively charted its properties. We asked a relatively large set of participants (n=38) to  
15 identify a briefly presented peripheral letter flanked by a single inward or outward letter at one  
16 of four locations. We also manipulated target location uncertainty and attentional allocation by  
17 blocking, randomising or precueing the target location. Using multi-level Bayesian regression  
18 analysis, we found robust IOA at all locations, although its strength was modulated by target  
19 location, location uncertainty and attentional allocation. Our findings suggest that IOA can be an  
20 excellent marker of crowding, to the extent that it is not observed in other flanker-interference  
21 mechanisms such as masking.

22 Keywords

23 Crowding; masking; inner-outer asymmetry; attention; location uncertainty

24

## 25 Introduction

26 Objects in clutter are hard to identify (Bouma, 1970; Levi, 2008). This phenomenon,  
27 known as visual crowding (Stuart & Burian, 1962), has been extensively studied over the past  
28 several decades and has provided valuable insights into several cognitive processes, including  
29 object recognition (Levi, 2008; Whitney & Levi, 2011), reading (Martelli et al., 2009; Pelli et al.,  
30 2007), and awareness (Atas et al., 2014; Kouider et al., 2011). However, deleterious interactions  
31 between an object and its flankers can also occur due to other spatial processes such as  
32 surround suppression and contrast masking (Levi et al., 2002; Pelli et al., 2004; Petrov et al.,  
33 2007). It has been suggested that crowding and contrast masking mechanisms can be  
34 distinguished by a set of properties: masking impairs detection, whereas crowding only affects  
35 identification; masking scales with the size of the objects, whereas crowding does not; masking  
36 is independent of eccentricity, whereas crowding is intimately dependent on it (Levi et al., 2002;  
37 Pelli et al., 2004).

38 Hence, the diagnostic test to determine if a particular target has suffered from crowding  
39 and not from masking was to check if the spatial extent of the target-flanker interaction scaled  
40 with eccentricity but not with stimulus size. If it did, then it was crowding. However, this set of  
41 diagnostic criteria was challenged by Petrov et al. (2007), who argued that surround suppression  
42 also had the same set of features. They proposed that the unique property differentiating  
43 crowding and surround suppression was that crowding displayed a specific sort of asymmetry  
44 known as In-Out Asymmetry (IOA) that surround suppression did not. IOA is the finding that the  
45 flanker farther away from the fovea (the 'outward' flanker) relative to the target interferes with  
46 target identification more than the flanker that is closer to the fovea (the 'inward' flanker). This  
47 appears counter-intuitive since the inward flanker should be more 'perceptible', because of  
48 better acuity for objects *closer* to the fovea, and hence should lead to more interference.  
49 However, a recent study has argued that an immediately adjacent outward flanker dominates  
50 perception under crowded conditions (Shechter & Yashar, 2021). The increased interference  
51 from the outward flanker is often explained as a consequence of cortical magnification, due to  
52 which neurons that respond to the outward flanker are closer to the neurons responding to the  
53 target than are the neurons responding to the inward flanker (Motter & Simoni, 2007; Pelli,  
54 2008), and hence cause more interference. Others have argued that the IOA can be attributed  
55 to the fact that receptive field sizes (within which interference occurs) increase with eccentricity

56 (Dayan and Solomon, 2010) or that a higher weight is assigned to the immediately outward  
57 flanker when sampling from available features (Shechter & Yashar, 2021).

58 IOA has been noticed and reported in a variety of settings right from the early days of  
59 crowding research (Banks et al., 1977; Bex et al., 2003; Estes et al., 1976; Krumhansl, 1977;  
60 Mackworth, 1965; See Strasburger, 2020 for a thorough historical exegesis of the phenomenon).  
61 Consequently, Petrov et al. (2007) proposed that a demonstration of IOA should be considered  
62 diagnostic of crowding.

63 However, IOA is not observed in all situations. For example, Petrov and Meleshkevich  
64 (2011b) found that IOA was present only along the horizontal meridian and not at other  
65 locations. In fact, most previous studies where IOA has been demonstrated also seem to have  
66 documented it along the horizontal meridian (Petrov et al., 2007; Petrov & Meleshkevich,  
67 2011a; Shechter & Yashar, 2021; Strasburger & Malania, 2013), whereas only a few studies have  
68 tested it at locations beyond the horizontal meridian (Petrov & Meleshkevich, 2011b; Bex et al.,  
69 2003). Even among the latter, one (Bex et al., 2003) did not actually test IOA at multiple  
70 locations, but instead tested stimuli that moved around a circular path around fixation (and  
71 therefore can be considered to be not restricted to the horizontal meridian). Hence there is not  
72 much evidence for IOA at locations beyond the horizontal meridian. Further, Petrov and  
73 Meleshkevich (2011b) showed that IOA was stronger if participants had to monitor two spatial  
74 locations than if the target was consistently presented at the same location. They argued that  
75 this effect could be ascribed to attentional deployment. That is, they contended that strong IOA  
76 is observed if (endogenous) attention is deployed to two locations but is weaker or absent if it is  
77 allocated to a single location, which is the case when the target is predictably presented at the  
78 same location. These findings would undermine the utility of IOA as a diagnostic indicator, since  
79 crowding is observed even if the target is always presented at the same location and also at  
80 locations other than the horizontal meridian. That is, if IOA cannot be observed in these  
81 circumstances, then it cannot serve as a diagnostic tool.

82 Further evidence for the role of attention in IOA was provided when, in a different study,  
83 Petrov and Meleshkevich (2011a) found that focusing attention to be at the target location  
84 (while the target could be at one of two locations) increased IOA, whereas diffusing attention by  
85 randomly jittering the target location over a small region decreased the strength of IOA.  
86 Additionally, when participants had to attend a central location, IOA was eliminated or even

87 reversed in some participants. This dependency (and indeed reversal) of IOA on the distribution  
88 of attention is another reason for a careful assessment of IOA as a diagnostic tool of crowding.

89 As discussed by Strasburger (2020), IOA appears to be reversed under some  
90 circumstances. When characters (letters or numerals) were used as stimuli, participants  
91 reported the inward flanker more often than the outward flanker in error trials (Chastain, 1982;  
92 Strasburger & Malania, 2013). These target-inward flanker confusions also scaled with  
93 eccentricity (Strasburger & Malania, 2013). These findings indicate that, when measured in a  
94 specific way, the effect of the inward flanker on the target appears to be stronger than that of  
95 the outward flanker. This seems to be the case when location uncertainty leads to whole objects  
96 being swapped among the target and its flankers. On the other hand, a recent study that used  
97 oriented Gabors combined with a continuous report measure found that the outward flanker is  
98 misreported far more often than the inward one when confusion does occur (Shechter &  
99 Yashar, 2021).

100 There are additional potential issues with the stimulus setup and participants generally  
101 used in these paradigms. Generally, these studies have been conducted with a *few, experienced*  
102 participants (which is often a good thing). Crucially, considerable inter-observer variability has  
103 been documented (Greenwood et al., 2017; Petrov & Meleshkevich, 2011b). If a property is to  
104 be considered diagnostic, it should be evident consistently in most, if not all, observers and not  
105 just the experienced. Incidentally, Petrov and Meleshkevich (2011a, 2011b) used coarsely  
106 discriminable stimuli (identifying Gabor orientations differing by 90°), which itself might result in  
107 little to no crowding (Pelli et al., 2004). This might have underestimated the strength and  
108 prevalence of IOA. Importantly, it could have concealed the existence of IOA in locations other  
109 than the horizontal meridian and for targets in predictable locations. Hence, stimulus choice  
110 might also be important in determining the robustness of IOA.

111 In the light of these inconsistent findings, can IOA be considered diagnostic of crowding?  
112 This study<sup>1</sup>, therefore, addresses a few related issues: 1) Can IOA be observed in (a relatively  
113 larger sample of) naïve observers? If so, what is its prevalence within this sample and how  
114 reliably can it be detected? 2) What is the strength of IOA and how variable is it across  
115 individuals? 3) Is IOA restricted to the horizontal meridian, as claimed by Petrov and  
116 Meleshkevich (2011b)? If so, it cannot be considered diagnostic of crowding. 4) It was suggested  
117 that IOA depends on attentional deployment; this study will also test if this is the case by

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<sup>1</sup> This study is part of a pre-registered project (the first experiment at this link: <https://osf.io/jdfmn/>)

118 directly manipulating attentional deployment using precues in a typical crowding paradigm.  
119 Finally, we will use letters as stimuli, which require fine discrimination and have been widely  
120 documented to be susceptible to crowding.

121 Importantly, we do not intend to question whether the extensively documented IOA  
122 exists or not, and as such, there is little value in carrying out standard null hypothesis testing.  
123 Instead, the aim of our study is to *measure* the size of the asymmetry, and how it varies across  
124 participants over a range of locations and manipulations. Therefore, to characterise IOA, we use  
125 Bayesian multi-level models which allow us to estimate the relevant parameters and the  
126 associated uncertainty.

## 127 Methods

### 128 Participants

129 Forty undergraduate students were recruited at two separate sites (20 at the University of  
130 Aberdeen and 20 at the University of Essex). All participants provided written informed consent  
131 and received monetary compensation. The study received prior approval by the respective local  
132 ethics boards and was conducted in accordance with the Declaration of Helsinki. All participants  
133 self-reported normal or corrected-to-normal vision. Two participants (Essex) did not complete  
134 all four sessions and hence were not included in our data analysis (final  $n = 38$ ). Initial reports  
135 (Petrov et al., 2007) suggested that crowding threshold elevation was four times higher for the  
136 ‘outward’ flankers compared to the ‘inward’ flankers, which is a large effect. Indeed, IOA was  
137 observable in each of the four participants tested. Later studies, when the effect was replicated,  
138 suggested slightly lower in-out ratios but still substantial enough to be observed in a few  
139 participants. Hence, a sample of 38 naïve participants, which is roughly three times larger than  
140 the largest sample tested previously<sup>2</sup>, should be sufficient to detect it, if it exists, and to  
141 characterise its nature and prevalence.

### 142 Materials and stimuli

143 Stimuli were generated using MATLAB (Mathworks, Natick, MA, USA) with Psychtoolbox  
144 extensions (Brainard, 1997; Kleiner et al., 2007; Pelli, 1997) and presented on LCD monitors (53  
145 cm width, 1920 x 1080 pixels, 60 Hz, University of Aberdeen; 47.6 cm width, 1920 x 1080 pixels,

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<sup>2</sup> We briefly note the sample sizes used in selected previous studies. Petrov et al., 2007: 5; Petrov and Meleshkevich, 2011a; Petrov and Meleshkevich, 2011b: 6; Shechter and Yashar, 2021: 13-14; Strasburger and Malania, 2013: 9-10.

146 60 Hz, University of Essex). A black square frame whose side was 5 pixels less than the height of  
147 the monitor was presented throughout the experiment to indicate the area within which the  
148 stimuli would be presented. Stimuli were nine black letters in the Sloan font (D, H, K, N, O, R, S,  
149 V and Z) presented on a grey background (Figure 1). The letter C was omitted since C and O are  
150 much less discriminable than other pairs in the Sloan font (Elliott et al., 1990; Song et al., 2014).  
151 One target and one flanker from this set were randomly chosen on any given trial. The target  
152 was presented at 7.5° eccentricity at one of four locations (left, right, above, or below the  
153 fixation, on the horizontal or vertical meridian). Pairs of white lines, of length 2° each, were  
154 presented on either side of the four possible target locations to reduce confusion about which  
155 of the two letters was the target. The lines were oriented perpendicular to the meridian across  
156 which they were arranged. The gap between these lines was set to twice the letter size (which  
157 was scaled on each trial; see below). We had piloted a version where the lines were fixed at the  
158 same locations on all trials, but observers reported that this still led to confusions regarding  
159 which of the letters was the target, particularly at small letter sizes. We believe that these lines  
160 would cause no or minimal crowding themselves, as they were aligned in the tangential  
161 direction and differed in contrast polarity, size, and complexity from the target (Kooi et al.,  
162 1994; Toet & Levi, 1992; Zhang et al., 2009).

163 A black fixation cross (0.3°) was presented throughout the trial. To ensure fixation, eye  
164 movements were monitored using a desktop mounted Eyelink 1000 eye tracker (SR Research  
165 Ltd, Mississauga, Ontario, Canada) with a sampling rate of 1000 Hz. The right eye was tracked,  
166 and a five-point calibration was performed at the beginning of each block. The same eye tracker  
167 make and model was used at both sides.

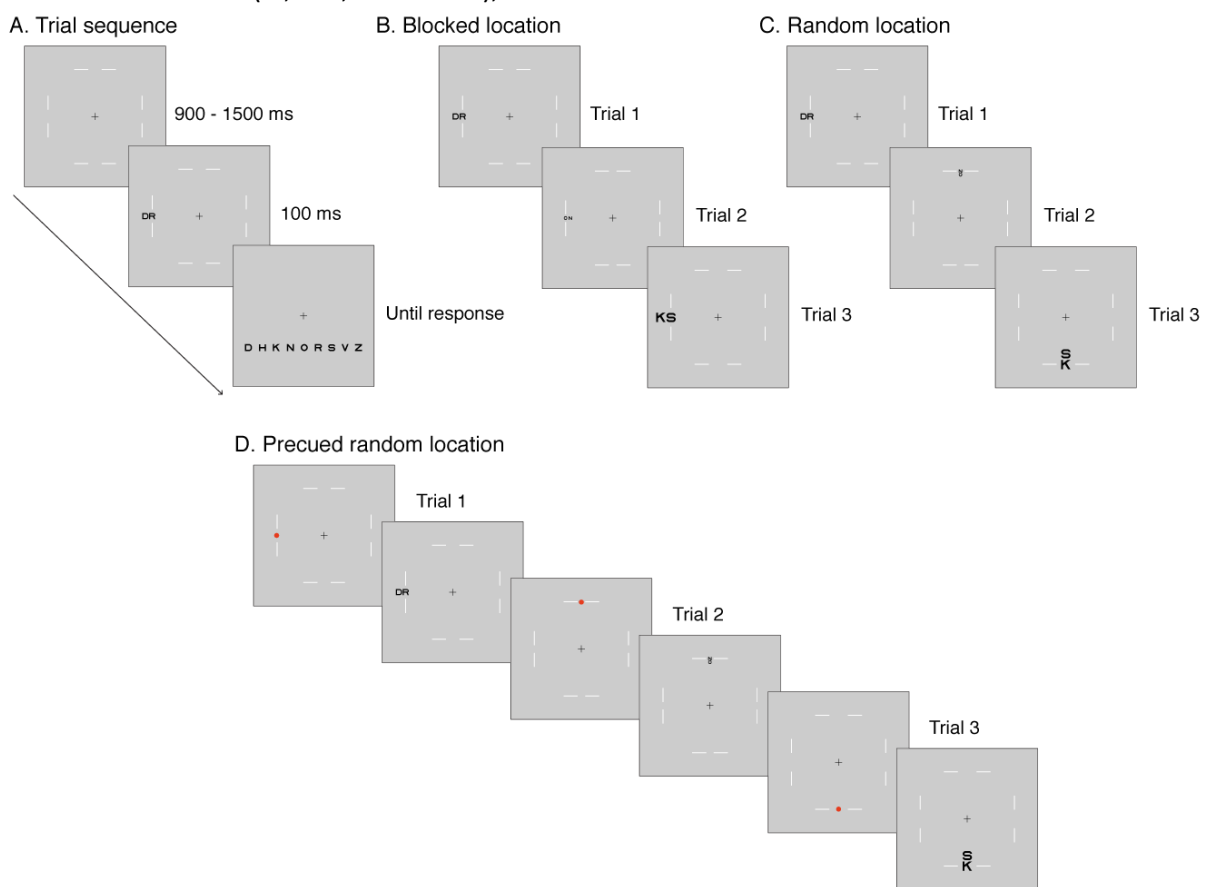
168 In some conditions a precue was presented at the location of the target to draw  
169 exogenous attention to that location (Nakayama & Mackeben, 1989). The precue was a red  
170 circle of diameter 0.3°, presented 100 ms before target onset and lasted for 50 ms.

## 171 Design

172 Participants were tested on three design conditions: *blocked*, *random*, and *precued*. In the  
173 blocked design condition, within a given block the target was presented at the same chosen  
174 location. In the random design condition, the target was presented in any of the four locations  
175 with equal probability. Finally, in the precued design condition the target was presented in any  
176 of the four locations with equal probability, but this location was indicated with a precue  
177 presented at the target location before target onset. Each design condition was tested in a

178 separate block and the order of blocks was randomised. Each participant completed eight blocks  
 179 of each design condition. These 24 blocks (3 design conditions x 8 blocks each) were tested over  
 180 four sessions (six blocks per session), which were in most cases run on separate days. Each block  
 181 included 120 trials, leading to a total of 2880 trials per participant.

182 The target was presented in isolation (unflanked) or along with a single flanker. When  
 183 presented, the flanker would be placed either on the inward (or foveal) side of the target or on  
 184 the outward (or peripheral) side of the target. All flanker locations (inward, outward, none)  
 185 were equally represented within each block. Overall, we assessed performance in three design  
 186 conditions (blocked, random, precue), four target locations (up, down, left, right) and three  
 187 flanker conditions (in, out, no flanker), for a total of 36 combinations.



188 **Figure 1: Trial sequence and stimulus conditions.** Panel A illustrates the temporal sequence of a typical trial.  
 189 After a fixation period between 900 – 1500 ms, the target and its flanker were presented for 100 ms. In this  
 190 example, a single ‘outward’ flanker was presented along with the target. However, in other trials, the flanker might  
 191 be presented on the ‘inward’ side or not presented (see panels C and D). The size of the letters (and hence spacing,  
 192 which is set as 1.1\*size) was controlled by the QUEST algorithm to determine flanked and unflanked acuity. All  
 193 possible letter identities were then presented for the participant to make a choice. B. Trials in the ‘Blocked location’  
 194 condition: targets were always presented at the same location within a block. C. Trials in the ‘Random location’  
 195 condition: targets and their flankers were presented in any of the four locations within the block. D. Trials in the  
 196 ‘Precue’ condition: a target was presented at a randomly chosen location, which was precued.

197 Procedure

198 Participants were seated 72 and 60 cm from the monitor, at the Aberdeen and Essex sites  
199 respectively, and their head was stabilised with a chin and forehead rest. In all conditions, each  
200 trial began with a variable fixation period of between 900 and 1500 ms in steps of 50 ms,  
201 randomly chosen. Fixation was monitored continuously with the eye-tracker. The trial was  
202 initiated only if the participant fixated within 100 pixels of the centre of the screen for 1000 ms.  
203 The target was then presented for 100 ms in isolation or with a single flanker placed either  
204 inwards or outwards relative to the target. All nine possible letter identities were then displayed  
205 on the screen and the participant reported the identity of the target letter with a mouse click.  
206 200 ms after the response, feedback was provided as a colour change of the fixation cross: it  
207 briefly (300 ms) turned green if the response was accurate and red if it was incorrect.

208 Following Song, et al. (2014) and Petrov and Meleshkevich (2011a, 2011b), we compared  
209 flanked with unflanked visual acuity to assess the extent of crowding in each of the 36 condition  
210 combinations. To do so, we first obtained acuity thresholds in each of the conditions using the  
211 QUEST algorithm, an adaptive staircase that controlled the size of the letters on a trial-by-trial  
212 basis. In the case of flanked acuity, the centre-to-centre spacing between the target and the  
213 flanker was fixed at 1.1 times the letter size, such that the spacing scaled with size, in order to  
214 prevent overlap and to measure the extent of crowding. The letter size was constrained to be  
215 between  $0.1^\circ$  and  $3^\circ$ , a relatively large range of sizes. The size threshold for each condition was  
216 estimated in two QUEST runs of 40 trials each. The 80 trials of these two runs were then pooled  
217 and (re)subjected to the QUEST algorithm to obtain a single threshold per condition. The  
218 parameters used for QUEST were: chance rate: 0.11 (one out of nine); slope of psychometric  
219 curve: 3.5; initial guess of acuity threshold:  $1.1^\circ$ ; standard deviation of the initial guess: 3; lapse  
220 rate: 0.05; threshold criterion: 0.5.

221 The ratio of flanked to unflanked acuity, called the crowding factor (Petrov &  
222 Meleshkevich, 2011a, 2011b), specifies the extent of crowding. A crowding factor of greater  
223 than one indicates the presence of crowding; the larger the factor, the larger the target-flanker  
224 interference zone. We then computed the ratio of crowding factors for outward and inward  
225 flankers, which is equivalent to computing the ratio between the size threshold in the presence  
226 of the outward flanker and the size threshold in the presence of the inward flanker. A ratio of  
227 greater than one indicates IOA, where the outward flanker is more effective at crowding than  
228 the inward flanker.



229 Data Analysis

230 In general, we have followed the advice on Bayesian modelling given by McElreath (2015).  
231 We used multilevel Bayesian linear regression (Bürkner, 2018), with a log-normal distribution, to  
232 model the relationship between *design* (blocks/randomised/precued), *location*  
233 (up/left/down/right), *flanker* (none/inwards/outwards) and a participant's letter identification  
234 *threshold*. All interactions were included, and all main effects were allowed to vary from  
235 observer to observer, allowing us to characterise in-out asymmetry and the variability of these  
236 estimates. We note that we did not log-transform the thresholds and fit the regression model to  
237 the transformed variables; instead, we assumed that the thresholds were drawn from a log-  
238 normal distribution rather than from a normal one. The log-normal distribution was used as the  
239 thresholds are bounded by zero and were expected to have a positive skew.

240 We used a set of informed conservative priors for our analysis, based on the following  
241 assumptions:

- 242 i) For the no-flanker condition, the thresholds for each of the four target locations  
243 were assigned  $N(1,2)$  priors, i.e., there is a 75% chance that the threshold lies  
244 between  $0.05^\circ$  and  $5^\circ$ , with a median of around  $1.6^\circ$ . Here and elsewhere  $N(\mu, \sigma)$   
245 represents a normal distribution with a mean of  $\mu$  and a standard deviation of  $\sigma$ .
- 246 ii) Threshold sizes in the flanked conditions are expected to be larger (Levi, 2008;  
247 Petrov & Meleshkevich, 2011a, 2011b). Since this study is intended to specifically  
248 investigate the difference between inwards and outwards flankers, we  
249 conservatively assumed that both effects are equal, and used a  $N(1, 0.5)$  distribution  
250 to describe them. These conditions were dummy coded, so this  $N(1, 0.5)$  distribution  
251 is combined with the intercept,  $N(1, 2)$  to give our prior predictions for these  
252 conditions. On average, we expect the thresholds in these conditions to be between  
253  $0.1^\circ$  and  $16^\circ$  with a median of around  $5.0^\circ$ .
- 254 iii) Similarly, since we are also interested in the effect of design condition and their  
255 interactions, we assigned a prior distribution of  $N(0, 1)$  for each condition.
- 256 iv) Group-level (random) effects were all assigned a weak half-Cauchy(0,10)  
257 distribution, while half-Cauchy(0,1) was used for the residual variance (Gelman,  
258 2006). These are often used as weak priors in Bayesian analysis as they rule out  
259 negative values (it is impossible to have a variance less than zero). Furthermore,

260 they capture our belief that the variance should be low, while the heavy tails mean  
261 that larger than expected values have not been ruled out.

262 Before training the model on our data, we carried out prior predictions to check that the  
263 above gave sensible predictions. For example, a prior prediction of a threshold of less than 0 or  
264 more than 100 degrees of visual angle would be implausible and hence the prior would be  
265 unacceptable. The priors listed above lead to a 75% Highest Density Interval of approximately  
266 [0.05, 15 degrees], which seems reasonable. Further details and full model specification, data  
267 and R code is available at <https://osf.io/jdfmn/>

268 The model was fit using R (v4.03; R Core Team, 2020) with the rStan (v 2.21.2; Carpenter  
269 et al., 2017) and brms (v2.14.4; Bürkner, 2017) packages. Highest posterior density intervals  
270 (HPDI) were calculated using the HDInterval package (v0.2.2).

## 271 Results

272 Thresholds estimated by QUEST with a standard deviation greater than 0.2 log units were  
273 discarded (Reuther & Chakravarthi, 2014), as these are not reliable. 61 out of 1368 thresholds  
274 (38 participants x 36 thresholds) were thus discarded (4%). A summary of these data is  
275 presented in Supplementary Table 1.1 (all supplementary materials are available as a html file at  
276 <https://osf.io/bcgz4/>).

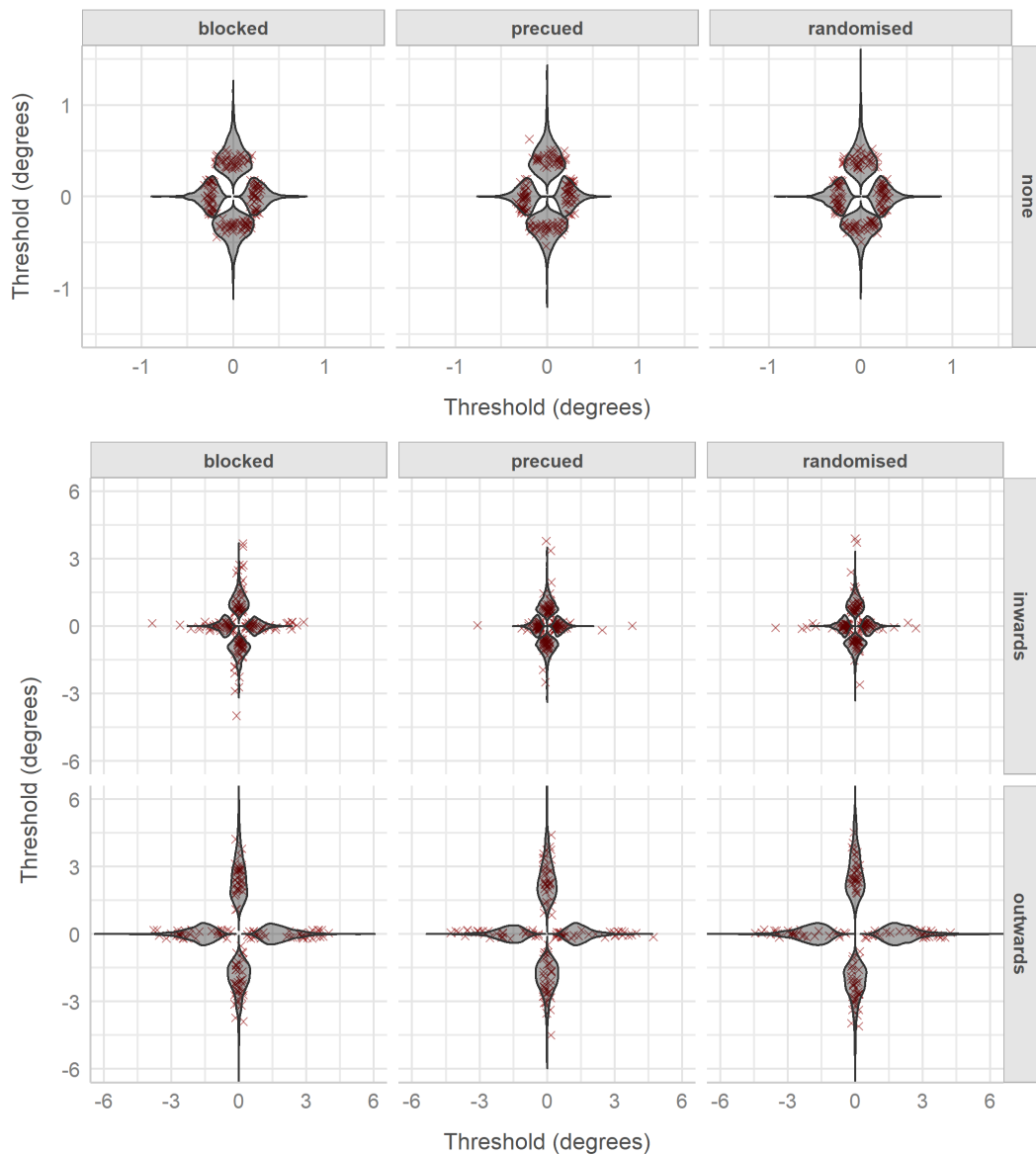
277 The multilevel lognormal model outlined in the data analysis section was successfully fit to  
278 these thresholds, with  $\hat{R} = 1$  for all parameters. The Bayesian  $R^2$  (Gelman et al., 2019) of the  
279 regression model, which is analogous to the standard  $R^2$ , was 0.78 (97% HPDI = [0.77, 0.79]). We  
280 proceed to analyse the model in more detail below.

281 Crowding and asymmetries in an average observer

### 282 *Crowding*

283 We first analysed the fixed effects of our model, i.e., the model's predictions for how the  
284 average observer would behave. Figure 2 shows that the addition of a flanker increased  
285 identification thresholds at all target locations and conditions. That is, both a single inward and  
286 a single outward flanker led to crowding. To quantify these observations, we computed the  
287 crowding factor, which is a measure of the strength of crowding (similar to the idea of threshold  
288 elevation), from the model's posterior distributions. The crowding factor is defined as the ratio  
289 between the size threshold in the presence of a flanker (either inwards or outwards) and the

290 threshold in the absence of a flanker (Figure 3, top row). Crowding factors were greater than 1  
 291 in all design conditions, target locations and flanker positions.



292 **Figure 2: Observed and estimated identification thresholds.** The top row presents size thresholds for  
 293 unflanked letters at each of four target locations (up, down, left and right) and three design conditions (blocked,  
 294 precued, randomised). The middle and bottom rows represent size thresholds for target letters flanked by inward  
 295 and outward letters, respectively. Note that the target letters were always presented at a distance of 7.5 degrees from  
 296 fixation in one of four locations. In all panels, each grey violin plot represents our model's posterior distribution of  
 297 threshold size for a target letter at that location (the size of the target that allowed an identification accuracy of  
 298 50%). The red x's represent individual observers' threshold. Note the difference in scale between the top row and  
 299 the other two (middle and bottom) rows.

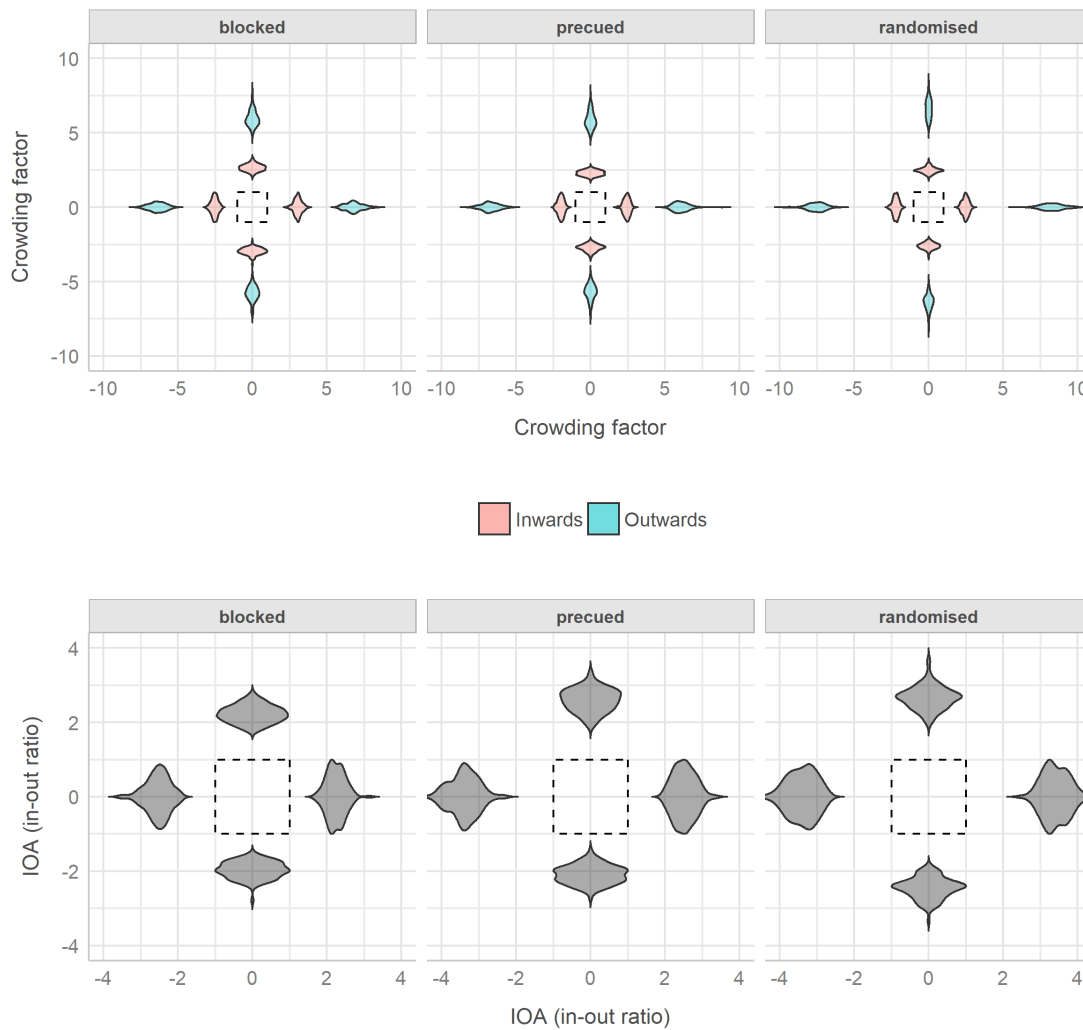
300 *In-Out Asymmetry (IOA)*

301 Importantly, Figure 3 (top row) shows that the crowding factors for the outward flanker  
 302 (turquoise) were larger than the factors for the inward flanker (pink). To quantify the extent of

303 this in-out-asymmetry (IOA), we computed the ratio between the size threshold in the outward  
 304 flanker condition and the threshold in the inward flanker condition (Figure 3, bottom row). Note  
 305 that this is equivalent to the ratio of crowding factors for the outward and inner flankers. The  
 306 plots show that the IOA was present in all conditions ( $p(\text{ioa} > 1 \mid \text{data}) > 0.99$ ) with identification  
 307 thresholds between 1.5 and 4.5 times larger when an outward flanker was present compared to  
 308 an inward flanker. Highest posterior density intervals (HPDI) are given for each condition in  
 309 Table 1. There clearly are differences in the strength of IOA across target locations and design  
 310 conditions. These are discussed below.

311 **Table 1: Characterising IOA.** The median in-out ratio, 53% and 97% HPDIs of the ratio in each design condition  
 312 and target location are shown. A ratio of greater than 1 indicates IOA, where an outward flanker causes more  
 313 crowding than an inward flanker. The first column indicates the probability of observing an IOA greater than 1.5 (a  
 314 conservative estimate of IOA). An IOA of at least 1.5 can be reliably observed in nearly all conditions. The  
 315 probability that the IOA ratio was greater than 1 was  $>0.99$  in all conditions and is not shown here. The remaining  
 316 columns indicate the range of the IOA ratio in our posterior predictions.

Location	Design	$p(\text{ioa}>1.5)$	Lower end of 97% HPDI	Lower end of 53% HPDI	Median	Upper end of 53% HPDI	Upper end of 97% HPDI
Right	Blocked	$>0.99$	1.74	2.10	2.21	2.45	2.76
	Precued	$>0.99$	1.96	2.24	2.50	2.66	3.10
	Random	$>0.99$	2.49	3.21	3.39	3.73	4.43
Up	Blocked	$>0.99$	1.79	2.08	2.21	2.42	2.70
	Precued	$>0.99$	1.90	2.46	2.62	2.91	3.12
	Random	$>0.99$	1.95	2.41	2.67	2.82	3.33
Left	Blocked	$>0.99$	1.93	2.30	2.51	2.69	3.30
	Precued	$>0.99$	2.33	3.06	3.38	3.55	4.22
	Random	$>0.99$	2.73	3.09	3.38	3.66	4.35
Down	Blocked	$>0.99$	1.55	1.74	1.97	2.07	2.39
	Precued	0.99	1.57	1.88	2.09	2.24	2.54
	Random	$>0.99$	1.91	2.27	2.41	2.63	3.01



317

318 **Figure 3: Crowding factors and in-out ratios.** The **top row** plots the posterior distributions of crowding factors  
 319 at each location and design condition for targets in the presence of either an inward (pink) or an outward (turquoise)  
 320 flanker. Crowding factor is defined as the ratio of size thresholds of a flanked target and an unflanked target. A ratio  
 321 of 1 (indicated by dashed lines at  $\pm 1$  in the plots) indicates no crowding. Any value greater than 1 indicates  
 322 crowding. It is evident that an outward flanker leads to stronger crowding than an inward flanker. The violin plots in  
 323 the **bottom row** represent the in-out ratio, which is ratio of the size threshold of a target flanked by an outward  
 324 letter and that of a target flanked by an inward letter. A ratio of more than 1 (indicated by dashed lines at  $\pm 1$ )  
 325 indicates IOA. IOA is evident in all locations and conditions.

326 *Visual field asymmetries in IOA*

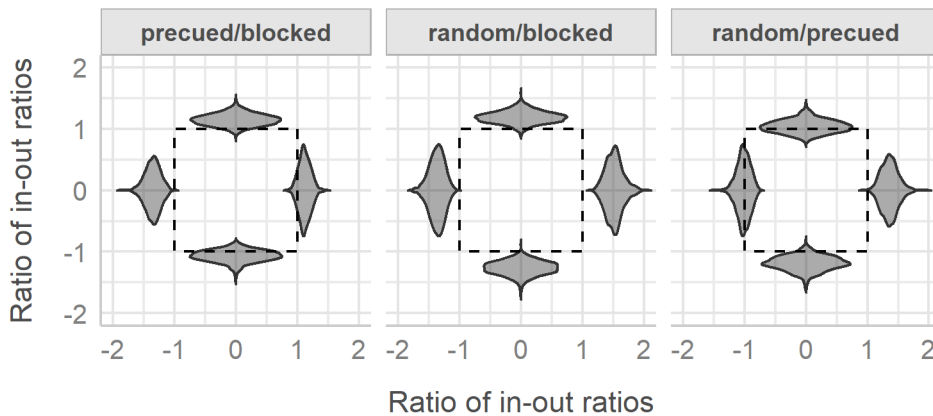
327 Recent studies on IOA presented inconsistent results in relation to its distribution across  
 328 the visual field. It was argued that it was chiefly observed along the horizontal meridian but not  
 329 at other locations (Petrov & Meleshkevich, 2011b). To characterise the pattern of IOA across the  
 330 visual field, we analysed the effect of target location. First, we computed the ratios between the  
 331 IOA at the *up* target location and the IOA in the *down* location. As we can do this repeatedly  
 332 using different samples from the model's posterior probability distribution, we can easily

333 compute the various conditional probabilities (Supplementary Table 4.2). IOA was stronger  
334 (more extreme) in the upper visual field compared to the lower visual field. This effect appears  
335 to be particularly robust in the blocked and pre-cued designs (both  $p = 0.98$ ), and much weaker  
336 ( $p \approx 0.7$ ) in the randomised condition. Similarly, IOA was stronger in the left visual field  
337 compared to the right, with a similar influence of design. Finally, we pooled the IOA ratios for  
338 locations along the horizontal meridian (left and right) and compared these to IOA ratios pooled  
339 along the vertical meridian (up and down). IOA was stronger along the horizontal meridian (left  
340 & right) compared to the vertical with  $p \geq 0.99$  across all three experimental designs. In  
341 summary, we found a Vertical Asymmetry, a Horizontal Asymmetry and a Horizontal-Vertical  
342 Asymmetry in IOA. However, as noted above, IOA was present at all locations.

#### 343 *The effect of attention and location uncertainty on IOA*

344 One of the motivations of the current study was to assess the effect of target location  
345 uncertainty on IOA. Previous studies had suggested that if targets were presented at a single  
346 location, IOA would be greatly diminished or disappear, whereas if the location was uncertain,  
347 IOA would be manifest, particularly along the horizontal meridian (Petrov & Meleshkevich,  
348 2011b). Further, modulating attentional allocation affected and sometimes even reversed the  
349 IOA (Petrov & Meleshkevich, 2011a). To test these observations, we assessed the differences in  
350 IOA across experimental designs (blocked, pre-cued and randomised). Figure 3 (bottom row)  
351 suggests that IOA was weaker in the blocked condition than in the randomised condition. This  
352 difference is more evident at horizontal locations compared to vertical ones. To quantify these  
353 observations, we computed pairwise ratios between IOA in the pre-cued, blocked and  
354 randomised conditions at each target location (Figure 4). When target locations were known for  
355 the entire block (blocked design), and hence voluntary attention could be allocated in advance,  
356 IOA was weaker than when attention was directed to the target location exogenously just  
357 before the target was presented (pre-cued). That is, reducing location uncertainty by diverting  
358 attention to the target location was not sufficient to render IOA comparable to when there was  
359 no location uncertainty. Exogenous attention can mitigate but not eliminate the asymmetry.  
360 Interestingly, precueing the location of the target had a nuanced effect on the strength of  
361 asymmetry compared to when location uncertainty was maximum (random target location). It  
362 reduced IOA at some locations (right and down) but not at others (left and up). Finally, IOA in  
363 the randomised target location condition was much stronger than in the blocked condition. That  
364 is, sustained attention to one location mitigated the IOA present when target location was

365 uncertain. In summary, IOA was strongest under conditions of target location uncertainty.  
 366 Precueing the target location and thus reducing target location uncertainty partially reduced the  
 367 asymmetry. However, advance knowledge of the target's location substantially reduced IOA.  
 368 Note that, importantly, IOA was not completely eliminated in any condition or location; at all  
 369 locations, the outward flanker was at least two times more effective at interfering with the  
 370 target than the inward flanker.



371  
 372 **Figure 4: The effect of design condition on IOA.** The ratio of in-out ratios between different design conditions  
 373 are depicted as violin plots. A ratio of 1 (dashed lines) marks no difference between design conditions.

374 Individual Differences in IOA

375 The fixed effects reported above give compelling evidence that there is IOA in the  
 376 “average participant”. However, as we can see from Figure 2 (red x's) there is substantial  
 377 variation in the identification thresholds across participants. To gain further insight into  
 378 individual differences, using our model we simulated a set of 1000 participants and calculated  
 379 the proportion of this sample that exhibits the IOA effects discussed above (Supplementary  
 380 Table 4.3). We found that a large majority of the new sample displayed IOA in all locations and  
 381 design conditions, suggesting that even when taking into account the fact that there are  
 382 considerable individual differences, the presence of IOA is reliable. The median and range of IOA  
 383 in this reconstructed sample was wider than that for the ‘average participant’. (By “average”,  
 384 we mean the fixed effect estimates discussed above, and not the raw empirical means). More  
 385 importantly for our main question of whether IOA can be considered a diagnostic marker of  
 386 crowding, there was a small minority of the sample in whom the IOA was not observed. This was  
 387 the case if we used a conservative criterion for establishing the asymmetry (that is, whether the  
 388 ratio of the effect of the outward flanker was 1.5 times that of the inward flanker). A less  
 389 stringent criterion (ratio > 1) indicated that IOA was observable in almost all participants at all

390 locations and conditions. The effect of target location and design appears to be the same as for  
391 the average participant.

392

### 393 Discussion

394 The In-Out Asymmetry (IOA) has been argued to be a diagnostic marker of crowding,  
395 superior to other previously considered criteria of crowding such as scaling with eccentricity in  
396 the absence of scaling with size (Petrov et al., 2007). However, there have been reports of  
397 inconsistencies in its strength and prevalence, both among individuals and across visual field  
398 locations (Petrov & Meleshkevich, 2011a, 2011b; Strasburger, 2020). Hence, we undertook a  
399 comprehensive study of IOA in a large cohort of participants at a range of visual field locations  
400 under multiple conditions. Our findings indicate that IOA is present in the vast majority of  
401 observers, locations and conditions. It is definitively present at all locations under diverse  
402 conditions of target uncertainty and attentional allocation when computed as an average across  
403 a population sample. However, there are considerable individual differences, with a small  
404 minority of individual participants not displaying or weakly displaying the asymmetry,  
405 particularly at some locations (e.g., lower visual field). These latter observations, however, are  
406 based on a conservative criterion applied to the estimated IOA as a measure of its presence (the  
407 proportion of a simulated population in whom the outward flanker's crowding effect is at least  
408 *1.5 times* that of the inward flanker's crowding effect). A more relaxed criterion (IOA ratio >1)  
409 shows that IOA is present at all locations under most conditions in the vast majority of  
410 individuals. Hence IOA can serve as a diagnostic marker of crowding across a sampled  
411 population and also among individuals, provided that this asymmetry is not observed in other  
412 flanker-induced interference phenomena such as masking (Petrov et al., 2007).

413 Our results indicate that IOA is modulated by attentional allocation. IOA was strongest  
414 when there was substantial target location uncertainty (target location randomly picked from  
415 among four possible options on each trial). However, in such a situation, if the target location  
416 was indicated by a brief precue, IOA was reduced at some, but not all, locations. That is,  
417 exogenous attention drawn to the target location, under conditions of location uncertainty,  
418 mitigates the in-out asymmetry at least in some locations. More interestingly, in situations  
419 where there was no target location uncertainty, and hence when sustained attention could be  
420 allocated to the location, the IOA was the weakest (albeit still observable). These findings  
421 suggest that the type and mode of attentional allocation modulates the strength of asymmetry.



422 Previous accounts have also found that attentional allocation modulates IOA, which have led to  
423 the proposal that the occurrence of IOA can be attributed to asymmetrical deployment of  
424 attention (Petrov & Meleshkevich, 2011a). Our findings are in line with this possibility but are  
425 also compatible with the proposal that there is biased sampling of the outward flanker  
426 (Shechter & Yashar, 2021). The latter argues that crowding arises due to pooling of features  
427 where a weighted sum of available features is taken within a receptive field. IOA arises in these  
428 circumstances because the immediately outward flanker is assigned a higher weight, leading to  
429 more frequent misreports of this flanker relative to other objects. While these two mechanisms  
430 implicitly point to different underlying mechanisms, in practical terms, they are hard to  
431 distinguish. An attentional bias towards the outer flanker can be argued to be equivalent to  
432 higher weights assigned to it. Further tests would be needed to disentangle the two. One issue  
433 with the disproportionate weighting hypothesis is that it is not clear how this would apply to  
434 complex objects, including letters. A weighted sum model can well explain crowding and IOA for  
435 simple features such as orientation and motion (Harrison & Bex, 2015; Shechter & Yashar, 2021;  
436 van den Berg et al., 2010), but the details for applying such a model to the relevant features of  
437 complex objects need to be worked out, although there have been impressive steps along this  
438 direction (Keshvari & Rosenholtz, 2016).

439 As noted above, IOA was observed at all tested locations, even when there was no  
440 location uncertainty of the target. Few studies have tested IOA at locations other than along the  
441 horizontal meridian. Petrov and colleagues (2011a, 2011b) reported that IOA was observed only  
442 along the horizontal meridian and only if multiple locations were monitored. The discrepancy  
443 between their results and ours can probably be attributed to a couple of factors: a) they used  
444 coarse discrimination tasks (2AFC) that might not have been sensitive enough to detect the  
445 slightly weaker IOA along the vertical meridian (and presumably other locations), b) sampling:  
446 we found that a minority of our participants do not exhibit IOA at some locations; it could be  
447 that previous studies might have inadvertently tested a small sample of participants with  
448 minimal or no IOA at some locations.

449 The strength of IOA is not the same across the visual field; that is, we observed a range of  
450 visual field asymmetries in IOA. IOA is stronger in the upper visual field than in the lower visual  
451 field (Vertical Asymmetry or VA); in the left visual field than in the right (Horizontal Asymmetry  
452 or HA); along the horizontal meridian than along the vertical meridian (Horizontal Vertical  
453 Asymmetry or HVA). These asymmetries are reminiscent of visual field asymmetries observed

454 across many visual tasks (Carrasco et al., 2001) including crowding. Crowding is known to be  
455 worse in the upper than in the lower visual field (VA; Intriligator & Cavanagh, 2001) and worse  
456 along the vertical meridian than along the horizontal meridian (HVA; Greenwood et al., 2017).  
457 Crowding is also worse in the left visual field than in the right visual field (HA; Greenwood et al.,  
458 2017; Kurzawski et al., 2021). At first glance, it might appear that the asymmetries in IOA are  
459 simply inherited from already prevalent asymmetries in crowding. However, it is clear from the  
460 above that, while there is some alignment in asymmetries, there are notable differences. Both  
461 IOA and crowding are stronger in the upper visual field compared to the lower visual field (VA).  
462 Similarly, both IOA and crowding are stronger in the left visual field than in the right (HA).  
463 However, IOA is stronger while crowding is *weaker* along the horizontal meridian than along the  
464 vertical (HVA). Further, the strongest asymmetry observed in crowding is the HVA (Kurzawski et  
465 al., 2021), which is the one that shows the reversal in asymmetry for IOA. This suggests that  
466 asymmetries in IOA are not simply inherited from crowding asymmetries. Nevertheless, it would  
467 be useful to keep in mind the admittedly more complex situation where the two asymmetries  
468 that do align are inherited, but the discrepant asymmetry (HVA) is affected by additional causes.  
469 This is not a parsimonious explanation, but our data are consistent with this possibility and  
470 hence it cannot be ruled out.

471         Some of the asymmetries in crowding have previously been explained in terms of  
472 attentional allocation, which might be taken to suggest that asymmetries in IOA can be  
473 attributed to asymmetries in attentional allocation. The resolution of attention is better in the  
474 lower visual field than in the upper visual field (Intriligator & Cavanagh, 2001). Performance in  
475 tasks that rely on sustained attention is also thought to be better along the horizontal meridian  
476 than along the vertical meridian (Mackeben, 1999). Further, while selective attention appears to  
477 work equally well in both left and right visual fields (Arguin et al., 1990; Corbetta et al., 1993;  
478 Yamaguchi et al., 1994), there is evidence that attention selects and processes stimuli better in  
479 the left visual field than in the right visual field (Asanowicz et al., 2013; Evert et al., 2003;  
480 Goodbourn & Holcombe, 2015; Matthews & Welch, 2015; Newman et al., 2017; Verleger et al.,  
481 2011). However, as with crowding asymmetries, the relationship between asymmetries in  
482 attentional tasks and those in IOA is inconsistent. Performance in attentional tasks is better  
483 along the horizontal meridian than along the vertical. Correspondingly, IOA is more extreme  
484 along the horizontal meridian than along the vertical. Further performance is often better in the  
485 left visual field than in the right, and IOA is stronger in the left visual field. In these cases, the  
486 strength of IOA and attentional allocation seem to be positively correlated. In contrast, although

487 the resolution of attention is better in the lower visual field relative to the upper visual field, IOA  
488 is less extreme in the lower visual field. Here, the strength of IOA seems to be inversely  
489 correlated with attentional allocation at these locations. That is, there does not seem to be a  
490 clear relationship between performance in attentional tasks and the strength of IOA, suggesting  
491 that attention cannot be the whole story. A nuance to this conclusion is the finding that when  
492 monitoring two rapid serial visual presentation streams, attention is better at selecting a target  
493 in the upper visual field than the one in the lower visual field target just as it preferentially  
494 selects a target in the left stream relative to the one on the right (Goodbourn & Holcombe,  
495 2015). This indicates better attentional selection in the left and upper visual fields compared to  
496 the right and lower visual fields, which might potentially explain the stronger IOA in these  
497 locations. This would account for all the observed asymmetries in IOA. However, such  
498 asymmetrical attentional processing was observed only when *two* locations were  
499 simultaneously monitored and was absent when a single stream was attended. In our  
500 experiment, we found the same pattern of IOA asymmetries irrespective of whether multiple  
501 locations had to be monitored (random design block) or when a single location was to be  
502 monitored for targets throughout the block (blocked design condition and arguably the precued  
503 design condition). Hence, the preferential attentional processing observed only when multiple  
504 simultaneous targets were monitored and reported might not help elucidate the mechanisms  
505 underlying the asymmetries observed in this study.

506 A speculative proposal to explain asymmetries in IOA is that the stronger asymmetry  
507 observed in the left visual field and also along the horizontal meridian might be due to the ease  
508 of processing letters at these locations acquired through years of reading experience (in  
509 languages that are read left to right, as was the case for the participants tested in this study).  
510 The participants might assign higher weights to the outermost letter(s) on the left side while  
511 reading, which leads to stronger IOA in the left visual field and a weaker one in the right visual  
512 field. The same reasoning can help explain the stronger IOA along the horizontal meridian  
513 relative to the vertical meridian. Since reading experience does not lead to higher weights to  
514 letters along the vertical meridian, the IOA along that axis tends to be weaker. Notwithstanding  
515 these possibilities, this 'reading experience' hypothesis does not explain the observed  
516 asymmetry between upper and lower visual fields (without some contortions).

517

518 Conclusion

519 We conducted an extensive examination of the in-out asymmetry in crowding in a  
520 relatively large sample of observers. The study was designed to characterise IOA at multiple  
521 visual field locations under various conditions of location uncertainty and attentional allocation.  
522 We found that the IOA is observable in all tested locations and conditions in the vast majority of  
523 participants. We conclude that it is a reasonable candidate to diagnose crowding to the extent  
524 that it can distinguish crowding from various other flanker-induced interference phenomena  
525 such as lateral masking, while keeping in mind that a small minority might not display the  
526 asymmetry at some locations.

527

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533

534 Author contributions

535 Conceptualisation: RC, ADFC; design and implementation: RC, ADFC; data collection: JR,  
536 NK; data analysis: ADFC, RC; writing: RC, ADFC; funding acquisition: RC.

537

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